

1. Use the graph below to answer the following questions.

a)
$$\lim_{x \to -3^{+}} f(x)$$

b) $\lim_{x \to -3^{-}} f(x)$
c) $\lim_{x \to -3^{-}} f(x)$
d) $\lim_{x \to -1} f(x)$
e) $\lim_{x \to 2} f(x)$
f) $\lim_{x \to -2} f(x)$
2. Determine each of the limits algebraically.
a) $\lim_{x \to -\infty} \frac{5x^{2} - 3x - 9}{2(4 - x)^{2}}$
b) $\lim_{x \to 5} \frac{x^{2} + 3x - 40}{2x - 10}$

c)
$$\lim_{x \to -3} \frac{2 - \sqrt{7 + x}}{x + 3}$$
 d) $\lim_{x \to 2} \begin{cases} x + 1 & x < 2 \\ \cos(\pi x) & x \ge 2 \end{cases}$

e)
$$\lim_{x \to -5} \frac{\frac{3}{x} + \frac{x+8}{5}}{x+5}$$
 f) $\lim_{x \to 0} \frac{\sin(4x)}{3x^2}$

3. Find the values of c so that the function
$$h(x) = \begin{cases} x^2 - c^2 & x < 2 \\ x + c & x \ge 2 \end{cases}$$
 is continuous.



4. Provide a function with the following criteria: f(0) > 0, f(2) < 0, but there are no zeros in the interval [0,2].

- 5. Create an equation with the given characteristics. There are two separate problems here, so there should be two different functions.
 - a) removable discontinuity at x = 3 and non-removable at x = -7.
 - b) $\lim_{x\to 0} f(x) = 3$ and f(0) = -1

6. Evaluate
$$\lim_{a \to 0} \frac{(x+a)^2 - x^2}{a}$$